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The Security Evaluated Standardized Password-Authenticated Key Exchange  
(SESPAKE) Protocol

Abstract

This document describes the Security Evaluated Standardized Password-Authenticated Key Exchange (SESPAKE) protocol. The SESPAKE protocol provides password-authenticated key exchange for usage in systems for protection of sensitive information. The security proofs of the protocol were made for situations involving an active adversary in the channel, including man-in-the-middle (MitM) attacks and attacks based on the impersonation of one of the subjects.

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## 1. Introduction

This document describes the Security Evaluated Standardized Password-Authenticated Key Exchange (SESPAKE) protocol. The SESPAKE protocol provides password-authenticated key exchange for usage in systems for protection of sensitive information. The protocol is intended to be used to establish keys that are then used to organize a secure channel for protection of sensitive information. The security proofs of the protocol were made for situations involving an active adversary in the channel, including man-in-the-middle (MitM) attacks and attacks based on the impersonation of one of the subjects.

## 2. Conventions Used in This Document

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [RFC2119].

### 3. Notations

This document uses the following parameters of elliptic curves in accordance with [RFC6090]:

- E an elliptic curve defined over a finite prime field  $GF(p)$ , where  $p > 3$ ;
- p the characteristic of the underlying prime field;
- a, b the coefficients of the equation of the elliptic curve in the canonical form;
- m the elliptic curve group order;
- q the elliptic curve subgroup order;
- P a generator of the subgroup of order q;
- X, Y the coordinates of the elliptic curve point in the canonical form;
- O zero point (point at infinity) of the elliptic curve.

This memo uses the following functions:

- HASH the underlying hash function;
- HMAC the function for calculating a message authentication code (MAC), based on a HASH function in accordance with [RFC2104];

F(PW, salt, n)  
the value of the function PBKDF2(PW, salt, n, len), where PBKDF2(PW, salt, n, len) is calculated according to [RFC8018]. The parameter len is considered equal to the minimum integer that is a multiple of 8 and satisfies the following condition:

len  $\geq$  floor(log<sub>2</sub>(q)).

This document uses the following terms and definitions for the sets and operations on the elements of these sets:

$B_n$  the set of byte strings of size  $n$ ,  $n \geq 0$ ; for  $n = 0$ , the  $B_n$  set consists of a single empty string of size 0; if  $b$  is an element of  $B_n$ , then  $b = (b_1, \dots, b_n)$ , where  $b_1, \dots, b_n$  are elements of  $\{0, \dots, 255\}$ ;

$||$  concatenation of byte strings  $A$  and  $C$ , i.e., if  $A$  in  $B_{n1}$ ,  $C$  in  $B_{n2}$ ,  $A = (a_1, a_2, \dots, a_{n1})$  and  $C = (c_1, c_2, \dots, c_{n2})$ , then  $A || C = (a_1, a_2, \dots, a_{n1}, c_1, c_2, \dots, c_{n2})$  is an element of  $B_{(n1 + n2)}$ ;

$\text{int}(A)$  for the byte string  $A = (a_1, \dots, a_n)$  in  $B_n$ , an integer  
 $\text{int}(A) = 256^{(n-1)}a_n + \dots + 256^{(0)}a_1$ ;

$\text{bytes}_n(X)$   
 the byte string  $A$  in  $B_n$ , such that  $\text{int}(A) = X$ , where  $X$  is an integer and  $0 \leq X < 256^n$ ;

$\text{BYTES}(Q)$   
 for  $Q$  in  $E$ , the byte string  $\text{bytes}_n(X) || \text{bytes}_n(Y)$ , where  $X, Y$  are standard Weierstrass coordinates of point  $Q$  and  $n = \text{ceil}(\log_{\{256\}}(p))$ .

#### 4. Protocol Description

The main point of the SESPAKE protocol is that parties sharing a weak key (a password) generate a strong common key. An active adversary who has access to a channel is not able to obtain any information that can be used to find a key in offline mode, i.e., without interaction with legitimate participants.

The protocol is used by subjects  $A$  (client) and  $B$  (server) that share some secret parameter that was established in an out-of-band mechanism: a client is a participant who stores a password as a secret parameter, and a server is a participant who stores a password-based computed point of the elliptic curve.

The SESPAKE protocol consists of two steps: the key-agreement step and the key-confirmation step. During the first step (the key-agreement step), the parties exchange keys using Diffie-Hellman with public components masked by an element that depends on the password -- one of the predefined elliptic curve points multiplied by the password-based coefficient. This approach provides an implicit key authentication, which means that after this step, one party is assured that no other party, aside from a specifically identified second party, may gain access to the generated secret key. During

the second step (the key-confirmation step), the parties exchange strings that strongly depend on the generated key. After this step, the parties are assured that a legitimate party, and no one else, actually has possession of the secret key.

To protect against online guessing attacks, counters that indicate the number of failed connections were introduced in the SESPAKE protocol. There is also a special technique for small-order point processing and a mechanism that provides protection against reflection attacks by using different operations for different sides.

#### 4.1. Protocol Parameters

Various elliptic curves can be used in the protocol. For each elliptic curve supported by clients, the following values MUST be defined:

- o the protocol parameters identifier, ID\_ALG (which can also define a HASH function, a pseudorandom function (PRF) used in the PBKDF2 function, etc.), which is a byte string of an arbitrary length;
- o the point P, which is a generator point of the subgroup of order q of the curve;
- o the set of distinct curve points  $\{Q_1, Q_2, \dots, Q_N\}$  of order q, where the total number of points, N, is defined for the protocol instance.

The method of generation of the points  $\{Q_1, Q_2, \dots, Q_N\}$  is described in Section 5.

The following protocol parameters are used by subject A:

1. The secret password value PW, which is a byte string that is uniformly randomly chosen from a subset of cardinality  $10^{10}$  or greater of the set  $B_k$ , where  $k \geq 6$  is the password length.
2. The list of curve identifiers supported by A.
3. Sets of points  $\{Q_1, Q_2, \dots, Q_N\}$ , corresponding to curves supported by A.
4. The  $C_1^A$  counter, which tracks the total number of unsuccessful authentication trials in a row, and a value of  $CLim_1$  that stores the maximum possible number of such events.

5. The  $C_2^A$  counter, which tracks the total number of unsuccessful authentication events during the period of usage of the specific PW, and a value of  $CLim_2$  that stores the maximum possible number of such events.
6. The  $C_3^A$  counter, which tracks the total number of authentication events (successful and unsuccessful) during the period of usage of the specific PW, and a value of  $CLim_3$  that stores the maximum possible number of such events.
7. The unique identifier,  $ID_A$ , of subject A (OPTIONAL), which is a byte string of an arbitrary length.

The following protocol parameters are used by subject B:

1. The values  $ind$  and  $salt$ , where  $ind$  is in  $\{1, \dots, N\}$  and  $salt$  is in  $\{1, \dots, 2^{128}-1\}$ .
2. The point  $Q_{PW}$ , satisfying the following equation:

$$Q_{PW} = \text{int}(F(PW, salt, 2000)) * Q_{ind}.$$

It is possible that the point  $Q_{PW}$  is not stored and is calculated using PW in the beginning of the protocol. In that case, B has to store PW and points  $\{Q_1, Q_2, \dots, Q_N\}$ .

3. The  $ID_{ALG}$  identifier.
4. The  $C_1^B$  counter, which tracks the total number of unsuccessful authentication trials in a row, and a value of  $CLim_1$  that stores the maximum possible number of such events.
5. The  $C_2^B$  counter, which tracks the total number of unsuccessful authentication events during the period of usage of the specific PW, and a value of  $CLim_2$  that stores the maximum possible number of such events.
6. The  $C_3^B$  counter, which tracks the total number of authentication events (successful and unsuccessful) during the period of usage of the specific PW, and a value of  $CLim_3$  that stores the maximum possible number of such events.
7. The unique identifier,  $ID_B$ , of subject B (OPTIONAL), which is a byte string of an arbitrary length.

#### 4.2. Initial Values of the Protocol Counters

After the setup of a new password value PW, the values of the counters MUST be assigned as follows:

- o  $C_1^A = C_1^B = \text{CLim}_1$ , where  $\text{CLim}_1$  is in  $\{3, \dots, 5\}$ ;
- o  $C_2^A = C_2^B = \text{CLim}_2$ , where  $\text{CLim}_2$  is in  $\{7, \dots, 20\}$ ;
- o  $C_3^A = C_3^B = \text{CLim}_3$ , where  $\text{CLim}_3$  is in  $\{10^3, 10^3+1, \dots, 10^5\}$ .

#### 4.3. Protocol Steps

The basic SESPAKE steps are shown in the scheme below:

A [A_ID, PW]		B [B_ID, Q_PW, ind, salt]
if $C_1^A$ or $C_2^A$ or $C_3^A = 0 \implies$ quit decrement $C_1^A, C_2^A, C_3^A$ by 1 $z_A = 0$	A_ID ----> <--- ID_ALG, B_ID (OPTIONAL), ind, salt	if $C_1^B$ or $C_2^B$ or $C_3^B = 0 \implies$ quit decrement $C_1^B, C_2^B, C_3^B$ by 1
$Q_{PW}^A = \text{int}(F(\text{PW}, \text{salt}, 2000)) * Q_{\text{ind}}$ choose alpha randomly from $\{1, \dots, q-1\}$ $u_1 = \text{alpha} * P - Q_{PW}^A$	$u_1 \text{ ---->}$	if $u_1$ not in E $\implies$ quit $z_B = 0$ $Q_B = u_1 + Q_{PW}$ choose beta randomly from $\{1, \dots, q-1\}$ if $m/q * Q_B = 0 \implies Q_B = \text{beta} * P, z_B = 1$ $K_B = \text{HASH}(\text{BYTES}((m/q * \text{beta} * (\text{mod } q)) * Q_B))$ $u_2 = \text{beta} * P + Q_{PW}$
if $u_2$ not in E $\implies$ quit $Q_A = u_2 - Q_{PW}^A$ if $m/q * Q_A = 0 \implies Q_A = \text{alpha} * P, z_A = 1$ $K_A = \text{HASH}(\text{BYTES}((m/q * \text{alpha}(\text{mod } q)) * Q_A))$	<--- $u_2$	

<pre> U_1 = BYTES(u_1), U_2 =   BYTES(u_2) MAC_A = HMAC(K_A, 0x01    ID_A    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A)  if MAC_B != HMAC(K_A, 0x02    ID_B    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A    DATA_B) ==&gt;   quit if z_A = 1 ==&gt; quit   C_1^A = CLim_1,   increment C_2^A by 1 </pre>	<pre> DATA_A, MAC_A ----&gt;  &lt;--- DATA_B, MAC_B </pre>	<pre> U_1 = BYTES(u_1), U_2 =   BYTES(u_2)  if MAC_A != HMAC(K_B, 0x01    ID_A    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A) ==&gt; quit if z_B = 1 ==&gt; quit C_1^B = CLim_1, increment   C_2^B by 1 MAC_B = HMAC(K_B, 0x02    ID_B    ind    salt    U_1    U_2    ID_ALG (OPTIONAL)    DATA_A    DATA_B) </pre>
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Table 1: SESPAKE Protocol Steps

The full description of the protocol consists of the following steps:

1. If any of the counters  $C_1^A$ ,  $C_2^A$ , or  $C_3^A$  is equal to 0, A finishes the protocol with an informational error regarding exceeding the number of trials that is controlled by the corresponding counter.
2. A decrements each of the counters  $C_1^A$ ,  $C_2^A$ , and  $C_3^A$  by 1, requests open authentication information from B, and sends the  $ID_A$  identifier.
3. If any of the counters  $C_1^B$ ,  $C_2^B$ , or  $C_3^B$  is equal to 0, B finishes the protocol with an informational error regarding exceeding the number of trials that is controlled by the corresponding counter.
4. B decrements each of the counters  $C_1^B$ ,  $C_2^B$ , and  $C_3^B$  by 1.



5. B sends the values of `ind`, `salt`, and the `ID_ALG` identifier to A. B also can `OPTIONALLY` send the `ID_B` identifier to A. All subsequent calculations are done by B in the elliptic curve group defined by the `ID_ALG` identifier.
6. A sets the curve defined by the received `ID_ALG` identifier as the used elliptic curve. All subsequent calculations are done by A in this elliptic curve group.
7. A calculates the point  $Q_{PW^A} = \text{int}(F(PW, \text{salt}, 2000)) * Q_{ind}$ .
8. A chooses randomly (according to the uniform distribution) the value `alpha`; `alpha` is in  $\{1, \dots, q-1\}$ ; then A assigns  $z_A = 0$ .
9. A sends the value  $u_1 = \text{alpha} * P - Q_{PW^A}$  to B.
10. After receiving `u_1`, B checks to see if `u_1` is in `E`. If it is not, B finishes with an error and considers the authentication process unsuccessful.
11. B calculates  $Q_B = u_1 + Q_{PW}$ , assigns  $z_B = 0$ , and chooses randomly (according to the uniform distribution) the value `beta`; `beta` is in  $\{1, \dots, q-1\}$ .
12. If  $m/q * Q_B = 0$ , B assigns  $Q_B = \text{beta} * P$  and  $z_B = 1$ .
13. B calculates  $K_B = \text{HASH}(\text{BYTES}((m/q * \text{beta} * (\text{mod } q)) * Q_B))$ .
14. B sends the value  $u_2 = \text{beta} * P + Q_{PW}$  to A.
15. After receiving `u_2`, A checks to see if `u_2` is in `E`. If it is not, A finishes with an error and considers the authentication process unsuccessful.
16. A calculates  $Q_A = u_2 - Q_{PW^A}$ .
17. If  $m/q * Q_A = 0$ , then A assigns  $Q_A = \text{alpha} * P$  and  $z_A = 1$ .
18. A calculates  $K_A = \text{HASH}(\text{BYTES}((m/q * \text{alpha} * (\text{mod } q)) * Q_A))$ .
19. A calculates  $U_1 = \text{BYTES}(u_1)$ ,  $U_2 = \text{BYTES}(u_2)$ .
20. A calculates  $\text{MAC}_A = \text{HMAC}(K_A, 0x01 || \text{ID}_A || \text{ind} || \text{salt} || U_1 || U_2 || \text{ID\_ALG (OPTIONAL)} || \text{DATA}_A)$ , where `DATA_A` is an `OPTIONAL` string that is authenticated with `MAC_A` (if it is not used, then `DATA_A` is considered to be of zero length).
21. A sends `DATA_A`, `MAC_A` to B.

22. B calculates  $U_1 = \text{BYTES}(u_1)$ ,  $U_2 = \text{BYTES}(u_2)$ .
23. B checks to see if the values  $\text{MAC}_A$  and  $\text{HMAC}(K_B, 0x01 || \text{ID}_A || \text{ind} || \text{salt} || U_1 || U_2 || \text{ID\_ALG (OPTIONAL)} || \text{DATA}_A)$  are equal. If they are not, it finishes with an error and considers the authentication process unsuccessful.
24. If  $z_B = 1$ , B finishes with an error and considers the authentication process unsuccessful.
25. B sets the value of  $C_1^B$  to  $\text{CLim}_1$  and increments  $C_2^B$  by 1.
26. B calculates  $\text{MAC}_B = \text{HMAC}(K_B, 0x02 || \text{ID}_B || \text{ind} || \text{salt} || U_1 || U_2 || \text{ID\_ALG (OPTIONAL)} || \text{DATA}_A || \text{DATA}_B)$ , where  $\text{DATA}_B$  is an OPTIONAL string that is authenticated with  $\text{MAC}_B$  (if it is not used, then  $\text{DATA}_B$  is considered to be of zero length).
27. B sends  $\text{DATA}_B$ ,  $\text{MAC}_B$  to A.
28. A checks to see if the values  $\text{MAC}_B$  and  $\text{HMAC}(K_A, 0x02 || \text{ID}_B || \text{ind} || \text{salt} || U_1 || U_2 || \text{ID\_ALG (OPTIONAL)} || \text{DATA}_A || \text{DATA}_B)$  are equal. If they are not, it finishes with an error and considers the authentication process unsuccessful.
29. If  $z_A = 1$ , A finishes with an error and considers the authentication process unsuccessful.
30. A sets the value of  $C_1^A$  to  $\text{CLim}_1$  and increments  $C_2^A$  by 1.

After the procedure finishes successfully, subjects A and B are mutually authenticated, and each subject has an explicitly authenticated value of  $K = K_A = K_B$ .

#### Notes:

1. In cases where the interaction process can be initiated by any subject (client or server), the  $\text{ID}_A$  and  $\text{ID}_B$  options MUST be used, and the receiver MUST check to see if the identifier he had received is not equal to his own; otherwise, it finishes the protocol. If an OPTIONAL parameter  $\text{ID}_A$  (or  $\text{ID}_B$ ) is not used in the protocol, it SHOULD be considered equal to a fixed byte string (a zero-length string is allowed) defined by a specific implementation.

2. The `ind`, `ID_A`, `ID_B`, and `salt` parameters can be agreed upon in advance. If some parameter is agreed upon in advance, it is possible not to send it during a corresponding step. Nevertheless, all parameters **MUST** be used as corresponding inputs to the HMAC function during Steps 20, 23, 26, and 28.
  3. The `ID_ALG` parameter can be fixed or agreed upon in advance.
  4. It is **RECOMMENDED** that the `ID_ALG` parameter be used in HMAC during Steps 20, 23, 26, and 28.
  5. Continuation of protocol interaction in a case where any of the counters  $C_1^A$  or  $C_1^B$  is equal to zero **MAY** be done without changing the password. In this case, these counters can be used for protection against denial-of-service attacks. For example, continuation of interaction can be allowed after a certain delay period.
  6. Continuation of protocol interaction in a case where any of the counters  $C_2^A$ ,  $C_3^A$ ,  $C_2^B$ , or  $C_3^B$  is equal to zero **MUST** be done only after changing the password.
  7. It is **RECOMMENDED** that during Steps 9 and 14 the points `u_1` and `u_2` be sent in a non-compressed format (`BYTES(u_1)` and `BYTES(u_2)`). However, point compression **MAY** be used.
  8. The use of several `Q` points can reinforce the independence of the data streams when working with several applications -- for example, when two high-level protocols can use two different points. However, the use of more than one point is **OPTIONAL**.
5. Construction of Points  $\{Q_1, \dots, Q_N\}$

This section provides an example of a possible algorithm for the generation of each point  $Q_i$  in the set  $\{Q_1, \dots, Q_N\}$  that corresponds to the given elliptic curve  $E$ .

The algorithm is based on choosing points with coordinates with known preimages of a cryptographic hash function  $H$ , which is the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output if  $2^{254} < q < 2^{256}$ , and the GOST R 34.11-2012 hash function (see [RFC6986]) with 512-bit output if  $2^{508} < q < 2^{512}$ .

The algorithm consists of the following steps:

1. Set  $i = 1$ ,  $SEED = 0$ ,  $s = 4$ .
2. Calculate  $X = \text{int}(\text{HASH}(\text{BYTES}(P) \parallel \text{bytes}_s(\text{SEED}))) \bmod p$ .
3. Check to see if the value of  $X^3 + aX + b$  is a quadratic residue in the field  $F_p$ . If it is not, set  $SEED = SEED + 1$  and return to Step 2.
4. Choose the value of  $Y = \min\{r_1, r_2\}$ , where  $r_1, r_2$  from  $\{0, 1, \dots, p-1\}$  are such that  $r_1 \neq r_2$  and  $r_1^2 = r_2^2 = R \bmod p$  for  $R = X^3 + aX + b$ .
5. Check to see if the following relations hold for the point  $Q = (X, Y)$ :  $Q \neq 0$  and  $q \cdot Q = 0$ . If they do, go to Step 6; if not, set  $SEED = SEED + 1$  and return to Step 2.
6. Set  $Q_i = Q$ . If  $i < N$ , then set  $i = i + 1$  and go to Step 2; otherwise, finish.

With the defined algorithm for any elliptic curve  $E$ , point sets  $\{Q_1, \dots, Q_N\}$  are constructed. Constructed points in one set MUST have distinct X-coordinates.

Note: The knowledge of a hash function preimage prevents knowledge of the multiplicity of any point related to generator point  $P$ . It is of primary importance, because such knowledge could be used to implement an attack against the protocol with an exhaustive search for the password.

## 6. Security Considerations

Any cryptographic algorithms -- particularly HASH functions and HMAC functions -- that are used in the SESPAKE protocol MUST be carefully designed and MUST be able to withstand all known types of cryptanalytic attacks.

It is RECOMMENDED that the HASH function satisfy the following condition:

- o  $\text{hashlen} \leq \log_2(q) + 4$ , where  $\text{hashlen}$  is the length of the HASH function output.

It is RECOMMENDED that the output length of hash functions used in the SESPAKE protocol be greater than or equal to 256 bits.

The points  $\{Q_1, Q_2, \dots, Q_N\}$  and  $P$  MUST be chosen in such a way that they are provably pseudorandom. As a practical matter, this means that the algorithm for generation of each point  $Q_i$  in the set  $\{Q_1, \dots, Q_N\}$  (see Section 5) ensures that the multiplicity of any point under any other point is unknown.

Using  $N = 1$  is RECOMMENDED.

Note: The specific adversary models for the protocol discussed in this document can be found in [SESPAKE-SECURITY], which contains the security proofs.

## 7. IANA Considerations

This document does not require any IANA actions.

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## 8.2. Informative References

- [RFC4357] Popov, V., Kurepkin, I., and S. Leontiev, "Additional Cryptographic Algorithms for Use with GOST 28147-89, GOST R 34.10-94, GOST R 34.10-2001, and GOST R 34.11-94 Algorithms", RFC 4357, DOI 10.17487/RFC4357, January 2006, <<http://www.rfc-editor.org/info/rfc4357>>.
- [SESPAKE-SECURITY] Smyshlyaev, S., Oshkin, I., Alekseev, E., and L. Ahmetzyanova, "On the Security of One Password Authenticated Key Exchange Protocol", 2015, <<http://eprint.iacr.org/2015/1237.pdf>>.

## Appendix A. Test Examples for GOST-Based Protocol Implementation

The following test examples are made for the protocol implementation that is based on the Russian national standards GOST R 34.10-2012 [GOST3410-2012] and GOST R 34.11-2012 [GOST3411-2012]. The English versions of these standards can be found in [RFC7091] and [RFC6986].

### A.1. Examples of Points

There is one point  $Q_1$  for each of the elliptic curves below. These points were constructed using the method described in Section 5 for  $N = 1$  and the GOST R 34.11-2012 hash function (see [RFC6986]). If  $2^{254} < q < 2^{256}$ , the GOST R 34.11-2012 hash function with 256-bit output is used, and if  $2^{508} < q < 2^{512}$ , the GOST R 34.11-2012 hash function with 512-bit output is used.

Each of the points complies with the GOST R 34.10-2012 [GOST3410-2012] standard and is represented by a pair of  $(X, Y)$  coordinates in the canonical form and also by a pair of  $(U, V)$  coordinates in the twisted Edwards form in accordance with [RFC7836] for the curves that have equivalent representations in this form. There is a SEED value for each point, by which it was generated.

`id-GostR3410-2001-CryptoPro-A-ParamSet`,  
`id-GostR3410-2001-CryptoPro-B-ParamSet`, etc. are defined in [RFC4357]. `id-tc26-gost-3410-2012-512-paramSetA`,  
`id-tc26-gost-3410-2012-512-paramSetB`, etc. are defined in [RFC7836].

#### A.1.1. Curve `id-GostR3410-2001-CryptoPro-A-ParamSet`

Point  $Q_1$

`X = 0xa69d51caf1a309fa9e9b66187759b0174c274e080356f23cfcbfe84d396ad7bb`  
`Y = 0x5d26f29ecc2e9ac0404dcf7986fa55fe94986362170f54b9616426a659786dac`  
`SEED = 0x0001`

#### A.1.2. Curve `id-GostR3410-2001-CryptoPro-B-ParamSet`

Point  $Q_1$

`X = 0x3d715a874a4b17cb3b517893a9794a2b36c89d2ffc693f01ee4cc27e7f49e399`  
`Y = 0x1c5a641fcf7ce7e87cdf8cea38f3db3096eace2fad158384b53953365f4fe7fe`  
`SEED = 0x0000`

#### A.1.3. Curve `id-GostR3410-2001-CryptoPro-C-ParamSet`

Point  $Q_1$

`X = 0x1e36383e43bb6cfa2917167d71b7b5dd3d6d462b43d7c64282ae67dfbec2559d`  
`Y = 0x137478a9f721c73932ea06b45cf72e37eb78a63f29a542e563c614650c8b6399`  
`SEED = 0x0006`



## A.1.4. Curve id-tc26-gost-3410-2012-512-paramSetA

Point Q<sub>1</sub>

```
X = 0x2a17f8833a32795327478871b5c5e88aefb91126c64b4b8327289bea62559425
    d18198f133f400874328b220c74497cd240586cb249e158532cb8090776cd61c
Y = 0x728f0c4a73b48da41ce928358fad26b47a6e094e9362bae82559f83cddc4ec3a
    4676bd3707edeaf4cd85e99695c64c241edc622be87dc0cf87f51f4367f723c5
SEED = 0x0001
```

## A.1.5. Curve id-tc26-gost-3410-2012-512-paramSetB

Point Q<sub>1</sub>

```
X = 0x7e1fae8285e035bec244bef2d0e5ebf436633cf50e55231dea9c9cf21d4c8c33
    df85d4305de92971f0a4b4c07e00d87bdbc720eb66e49079285aaf12e0171149
Y = 0x2cc89998b875d4463805ba0d858a196592db20ab161558ff2f4ef7a85725d209
    53967ae621afdeae89bb77c83a2528ef6f6ce02f68bda4679d7f2704947dbc408
SEED = 0x0000
```

## A.1.6. Curve id-tc26-gost-3410-2012-256-paramSetA

Point Q<sub>1</sub>

```
X = 0xb51adf93a40ab15792164fad3352f95b66369eb2a4ef5efae32829320363350e
Y = 0x74a358cc08593612f5955d249c96afb7e8b0bb6d8bd2bbe491046650d822be18
U = 0xebe97afffe0d0f88b8b0114b8de430ac2b34564e4420af24728e7305bc48aeaa
V = 0x828f2dcf8f06612b4fea4da72ca509c0f76dd37df424ea22bfa6f4f65748c1e4
SEED = 0x0001
```

## A.1.7. Curve id-tc26-gost-3410-2012-512-paramSetC

Point Q<sub>1</sub>

```
X = 0x489c91784e02e98f19a803abca319917f37689e5a18965251ce2ff4e8d8b298f
    5ba7470f9e0e713487f96f4a8397b3d09a270c9d367eb5e0e6561adeeb51581d
Y = 0x684ea885aca64eaf1b3fee36c0852a3be3bd8011b0ef18e203ff87028d6eb5db
    2c144a0dcc71276542bfd72ca2a43fa4f4939da66d9a60793c704a8c94e16f18
U = 0x3a3496f97e96b3849a4fa7db60fd93858bde89958e4beebd05a6b3214216b37c
    9d9a560076e7ea59714828b18fbfef996ffc98bf3dc9f2d3cb0ed36a0d6ace88
V = 0x52d884c8bf0ad6c5f7b3973e32a668daalf1ed092eff138dae6203b2ccdec561
    47464d35fec4b727b2480eb143074712c76550c7a54ff3ea26f70059480dcb50
SEED = 0x0013
```

## A.2. Test Examples of SESPAKE

This protocol implementation uses the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output as the H function and the HMAC\_GOSTR3411\_2012\_512 function defined in [RFC7836] as a PRF for the F function. The parameter len is considered equal to 256 if  $2^{254} < q < 2^{256}$ , and equal to 512 if  $2^{508} < q < 2^{512}$ .

The test examples for the point of each curve in Appendix A.1 are given below.

#### A.2.1. Curve id-GostR3410-2001-CryptoPro-A-ParamSet

The input protocol parameters in this example take the following values:

```

N = 1
ind = 1
ID_A:
  00 00 00 00
ID_B:
  00 00 00 00
PW:
  31 32 33 34 35 36 ('123456')
salt:
  29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q_ind:
  X = 0xA69D51CAF1A309FA9E9B66187759B0174C274E080356F23CFCBFE84D396AD7BB
  Y = 0x5D26F29ECC2E9AC0404DCF7986FA55FE94986362170F54B9616426A659786DAC

```

The function  $F(\text{PW}, \text{salt}, 2000)$  takes the following values:

```

F(PW, salt, 2000):
  BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
  D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67

```

The coordinates of the point  $Q_{\text{PW}}$  are:

```

  X = 0x59495655D1E7C7424C622485F575CCF121F3122D274101E8AB734CC9C9A9B45E
  Y = 0x48D1C311D33C9B701F3B03618562A4A07A044E3AF31E3999E67B487778B53C62

```

During the calculation of  $u_1$  on subject A, the parameter alpha, the point  $\text{alpha} * P$ , and  $u_1$  take the following values:

```

alpha=0x1F2538097D5A031FA68BBB43C84D12B3DE47B7061C0D5E24993E0C873CDBA6B3
alpha*P:
  X = 0xBBC77CF42DC1E62D06227935379B4AA4D14FEA4F565DDF4CB4FA4D31579F9676
  Y = 0x8E16604A4AFDF28246684D4996274781F6CB80ABBBA1414C1513EC988509DABF
u_1:
  X = 0x204F564383B2A76081B907F3FCA8795E806BE2C2ED228730B5B9E37074229E8D
  Y = 0xE84F9E442C61DDE37B601A7F37E7CA11C56183FA071DFA9320EDE3E7521F9D41

```

When processing `u_1`, calculating the `K_B` key, and calculating `u_2` on subject B, the parameters `beta`, `src`, `K_B = HASH(src)`, `beta*P`, and `u_2` take the following values:

`beta=0xDC497D9EF6324912FD367840EE509A2032AEDB1C0A890D133B45F596FCCBD45D`

`src:`

```
2E 01 A3 D8 4F DB 7E 94 7B B8 92 9B E9 36 3D F5
F7 25 D6 40 1A A5 59 D4 1A 67 24 F8 D5 F1 8E 2C
A0 DB A9 31 05 CD DA F4 BF AE A3 90 6F DD 71 9D
BE B2 97 B6 A1 7F 4F BD 96 DC C7 23 EA 34 72 A9
```

`K_B:`

```
1A 62 65 54 92 1D C2 E9 2B 4D D8 D6 7D BE 5A 56
62 E5 62 99 37 3F 06 79 95 35 AD 26 09 4E CA A3
```

`beta*P:`

```
X = 0x6097341C1BE388E83E7CA2DF47FAB86E2271FD942E5B7B2EB2409E49F742BC29
Y = 0xC81AA48BDB4CA6FA0EF18B9788AE25FE30857AA681B3942217F9FED151BAB7D0
```

`u_2:`

```
X = 0xDC137A2F1D4A35AEBC0ECBF6D3486DEF8480BFDC752A86DD4F207D7D1910E22D
Y = 0x7532F0CE99DCC772A4D77861DAE57C138F07AE304A727907FB0AAFDB624ED572
```

When processing `u_2` and calculating the key on subject A, the `K_A` key takes the following values:

`K_A:`

```
1A 62 65 54 92 1D C2 E9 2B 4D D8 D6 7D BE 5A 56
62 E5 62 99 37 3F 06 79 95 35 AD 26 09 4E CA A3
```

The message `MAC_A = HMAC(K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)` from subject A takes the following values:

`MAC_A:`

```
23 7A 03 C3 5F 49 17 CE 86 B3 58 94 45 F1 1E 1A
6F 10 8B 2F DD 0A A9 E8 10 66 4B 25 59 60 B5 79
```

The message `MAC_B = HMAC(K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)` from subject B takes the following values:

`MAC_B:`

```
9E E0 E8 73 3B 06 98 50 80 4D 97 98 73 1D CD 1C
FF E8 7A 3B 15 1F 0A E8 3E A9 6A FB 4F FC 31 E4
```

## A.2.2. Curve id-GostR3410-2001-CryptoPro-B-ParamSet

The input protocol parameters in this example take the following values:

```

N = 1
ind = 1
ID_A:
  00 00 00 00
ID_B:
  00 00 00 00
PW:
  31 32 33 34 35 36 ('123456')
salt:
  29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q_ind:
  X = 0x3D715A874A4B17CB3B517893A9794A2B36C89D2FFC693F01EE4CC27E7F49E399
  Y = 0x1C5A641FCF7CE7E87CDF8CEA38F3DB3096EACE2FAD158384B53953365F4FE7FE

```

The function  $F(\text{PW}, \text{salt}, 2000)$  takes the following values:

```

F(PW, salt, 2000):
  BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
  D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67

```

The coordinates of the point  $Q_{\text{PW}}$  are:

```

X = 0x6DC2AE26BC691FCA5A73D9C452790D15E34BA5404D92955B914C8D2662ABB985
Y = 0x3B02AAA9DD65AE30C335CED12F3154BBAC059F66B088306747453EDF6E5DB077

```

During the calculation of  $u_1$  on subject A, the parameter  $\alpha$ , the point  $\alpha * P$ , and  $u_1$  take the following values:

```

alpha=0x499D72B90299CAB0DA1F8BE19D9122F622A13B32B730C46BD0664044F2144FAD
alpha*P:
  X = 0x61D6F916DB717222D74877F179F7EBEF7CD4D24D8C1F523C048E34A1DF30F8DD
  Y = 0x3EC48863049CFCFE662904082E78503F4973A4E105E2F1B18C69A5E7FB209000
u_1:
  X = 0x21F5437AF33D2A1171A070226B4AE82D3765CD0EEBFF1ECEFE158EBC50C63AB1
  Y = 0x5C9553B5D11AAAECE738AD9A9F8CB4C100AD4FA5E089D3CBCCEA8C0172EB7ECC

```

When processing `u_1`, calculating the `K_B` key, and calculating `u_2` on subject B, the parameters `beta`, `src`, `K_B = HASH(src)`, `beta*P`, and `u_2` take the following values:

`beta=0x0F69FF614957EF83668EDC2D7ED614BE76F7B253DB23C5CC9C52BF7DF8F4669D`

`src:`

```
50 14 0A 5D ED 33 43 EF C8 25 7B 79 E6 46 D9 F0
DF 43 82 8C 04 91 9B D4 60 C9 7A D1 4B A3 A8 6B
00 C4 06 B5 74 4D 8E B1 49 DC 8E 7F C8 40 64 D8
53 20 25 3E 57 A9 B6 B1 3D 0D 38 FE A8 EE 5E 0A
```

`K_B:`

```
A6 26 DE 01 B1 68 0F F7 51 30 09 12 2B CE E1 89
68 83 39 4F 96 03 01 72 45 5C 9A E0 60 CC E4 4A
```

`beta*P:`

```
X = 0x33BC6F7E9C0BA10CFB2B72546C327171295508EA97F8C8BA9F890F2478AB4D6C
Y = 0x75D57B396C396F492F057E9222CCC686437A2AAD464E452EF426FC8EEED1A4A6
```

`u_2:`

```
X = 0x089DDEE718EE8A224A7F37E22CFFD731C25FCBF58860364EE322412CDCEF99AC
Y = 0x0ECE03D4E395A6354C571871BEF425A532D5D463B0F8FD427F91A43E20CDA55C
```

When processing `u_2` and calculating the key on subject A, the `K_A` key takes the following values:

`K_A:`

```
A6 26 DE 01 B1 68 0F F7 51 30 09 12 2B CE E1 89
68 83 39 4F 96 03 01 72 45 5C 9A E0 60 CC E4 4A
```

The message `MAC_A = HMAC(K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)` from subject A takes the following values:

`MAC_A:`

```
B9 1F 43 90 2A FA 90 D3 E5 C6 91 CB DC 43 8A 1E
BF 54 7F 4C 2C B4 14 43 CC 38 79 7B E2 47 A7 D0
```

The message `MAC_B = HMAC(K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)` from subject B takes the following values:

`MAC_B:`

```
79 D5 54 83 FD 99 B1 2B CC A5 ED C6 BB E1 D7 B9
15 CE 04 51 B0 89 1E 77 5D 4A 61 CB 16 E3 3F CC
```

## A.2.3. Curve id-GostR3410-2001-CryptoPro-C-ParamSet

The input protocol parameters in this example take the following values:

```

N = 1
ind = 1
ID_A:
  00 00 00 00
ID_B:
  00 00 00 00
PW:
  31 32 33 34 35 36 ('123456')
salt:
  29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q_ind:
  X = 0x1E36383E43BB6CFA2917167D71B7B5DD3D6D462B43D7C64282AE67DFBEC2559D
  Y = 0x137478A9F721C73932EA06B45CF72E37EB78A63F29A542E563C614650C8B6399

```

The function  $F(\text{PW}, \text{salt}, 2000)$  takes the following values:

```

F(PW, salt, 2000):
  BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
  D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67

```

The coordinates of the point  $Q_{\text{PW}}$  are:

```

X = 0x945821DAF91E158B839939630655A3B21FF3E146D27041E86C05650EB3B46B59
Y = 0x3A0C2816AC97421FA0E879605F17F0C9C3EB734CFF196937F6284438D70BDC48

```

During the calculation of  $u_1$  on subject A, the parameter  $\alpha$ , the point  $\alpha * P$ , and  $u_1$  take the following values:

```

alpha=0x3A54AC3F19AD9D0B1EAC8ACDCEA70E581F1DAC33D13FEAFD81E762378639C1A8
alpha*P:
  X = 0x96B7F09C94D297C257A7DA48364C0076E59E48D221CBA604AE111CA3933B446A
  Y = 0x54E4953D86B77ECCEB578500931E822300F7E091F79592CA202A020D762C34A6
u_1:
  X = 0x81BBD6FCA464D2E2404A66D786CE4A777E739A89AEB68C2DAC99D53273B75387
  Y = 0x6B6DBD922EA7E060998F8B230AB6EF07AD2EC86B2BF66391D82A30612EADD411

```

When processing `u_1`, calculating the `K_B` key, and calculating `u_2` on subject B, the parameters `beta`, `src`, `K_B = HASH(src)`, `beta*P`, and `u_2` take the following values:

`beta=0x448781782BF7C0E52A1DD9E6758FD3482D90D3CFCCF42232CF357E59A4D49FD4`

`src:`

```
16 A1 2D 88 54 7E 1C 90 06 BA A0 08 E8 CB EC C9
D1 68 91 ED C8 36 CF B7 5F 8E B9 56 FA 76 11 94
D2 8E 25 DA D3 81 8D 16 3C 49 4B 05 9A 8C 70 A5
A1 B8 8A 7F 80 A2 EE 35 49 30 18 46 54 2C 47 0B
```

`K_B:`

```
BE 7E 7E 47 B4 11 16 F2 C7 7E 3B 8F CE 40 30 72
CA 82 45 0D 65 DE FC 71 A9 56 49 E4 DE EA EC EE
```

`beta*P:`

```
X = 0x4B9C0AB55A938121F282F48A2CC4396EB16E7E0068B495B0C1DD4667786A3EB7
Y = 0x223460AA8E09383E9DF9844C5A0F2766484738E5B30128A171B69A77D9509B96
```

`u_2:`

```
X = 0x2ED9B903254003A672E89EBEBC9E31503726AD124BB5FC0A726EE0E6FCCE323E
Y = 0x4CF5E1042190120391EC8DB62FE25E9E26EC60FB0B78B242199839C295FCD022
```

When processing `u_2` and calculating the key on subject A, the `K_A` key takes the following values:

`K_A:`

```
BE 7E 7E 47 B4 11 16 F2 C7 7E 3B 8F CE 40 30 72
CA 82 45 0D 65 DE FC 71 A9 56 49 E4 DE EA EC EE
```

The message `MAC_A = HMAC(K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)` from subject A takes the following values:

`MAC_A:`

```
D3 B4 1A E2 C9 43 11 36 06 3E 6D 08 A6 1B E9 63
BD 5E D6 A1 FF F9 37 FA 8B 09 0A 98 E1 62 BF ED
```

The message `MAC_B = HMAC(K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)` from subject B takes the following values:

`MAC_B:`

```
D6 B3 9A 44 99 BE D3 E0 4F AC F9 55 50 2D 16 B2
CB 67 4A 20 5F AC 3C D8 3D 54 EC 2F D5 FC E2 58
```

## A.2.4. Curve id-tc26-gost-3410-2012-512-paramSetA

The input protocol parameters in this example take the following values:

```
N = 1
ind = 1
ID_A:
  00 00 00 00
ID_B:
  00 00 00 00
PW:
  31 32 33 34 35 36 ('123456')
salt:
  29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q_ind:
  X = 0x2A17F8833A32795327478871B5C5E88AEFB91126C64B4B8327289BEA62559425
    D18198F133F400874328B220C74497CD240586CB249E158532CB8090776CD61C
  Y = 0x728F0C4A73B48DA41CE928358FAD26B47A6E094E9362BAE82559F83CDDC4EC3A
    4676BD3707EDEAF4CD85E99695C64C241EDC622BE87DC0CF87F51F4367F723C5
```

The function  $F(\text{PW}, \text{salt}, 2000)$  takes the following values:

```
F(PW, salt, 2000):
  BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
  D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
  1C 62 13 E3 93 0E FD DA 26 45 17 92 C6 20 81 22
  EE 60 D2 00 52 0D 69 5D FD 9F 5F 0F D5 AB A7 02
```

The coordinates of the point  $Q_{\text{PW}}$  are:

```
X = 0x0C0AB53D0E0A9C607CAD758F558915A0A7DC5DC87B45E9A58FDDF30EC3385960
  283E030CD322D9E46B070637785FD49D2CD711F46807A24C40AF9A42C8E2D740
Y = 0xDF93A8012B86D3A3D4F8A4D487DA15FC739EB31B20B3B0E8C8C032AAF8072C63
  37CF7D5B404719E5B4407C41D9A3216A08CA69C271484E9ED72B8AAA52E28B8B
```



During the calculation of  $u_1$  on subject A, the parameter  $\alpha$ , the point  $\alpha^*P$ , and  $u_1$  take the following values:

```
alpha=0x3CE54325DB52FE798824AEAD11BB16FA766857D04A4AF7D468672F16D90E7396
046A46F815693E85B1CE5464DA9270181F82333B0715057BBE8D61D400505F0E
alpha*P:
  X = 0xB93093EB0FCC463239B7DF276E09E592FCFC9B635504EA4531655D76A0A3078E
    2B4E51CFE2FA400CC5DE9FBE369DB204B3E8ED7EDD85EE5CCA654C1AED70E396
  Y = 0x809770B8D910EA30BD2FA89736E91DC31815D2D9B31128077EEDC371E9F69466
    F497DC64DD5B1FADC587F860EE256109138C4A9CD96B628E65A8F590520FC882
u_1:
  X = 0xE7510A9EDD37B869566C81052E2515E1563FDFE79F1D782D6200F33C3CC2764D
    40D0070B73AD5A47BAE9A8F2289C1B07DAC26A1A2FF9D3ECB0A8A94A4F179F13
  Y = 0xBA333B912570777B626A5337BC7F727952460EEBA2775707FE4537372E902DF5
    636080B25399751BF48FB154F3C2319A91857C23F39F89EF54A8F043853F82DE
```

When processing  $u_1$ , calculating the  $K_B$  key, and calculating  $u_2$  on subject B, the parameters  $\beta$ ,  $\text{src}$ ,  $K_B = \text{HASH}(\text{src})$ ,  $\beta^*P$ , and  $u_2$  take the following values:

```
beta=0xB5C286A79AA8E97EC0E19BC1959A1D15F12F8C97870BA9D68CC12811A56A3BB1
1440610825796A49D468CDC9C2D02D76598A27973D5960C5F50BCE28D8D345F4
src:
 84 59 C2 0C B5 C5 32 41 6D B9 28 EB 50 C0 52 0F
 B2 1B 9C D3 9A 4E 76 06 B2 21 BE 15 CA 1D 02 DA
 08 15 DE C4 49 79 C0 8C 7D 23 07 AF 24 7D DA 1F
 89 EC 81 20 69 F5 D9 CD E3 06 AF F0 BC 3F D2 6E
 D2 01 B9 53 52 A2 56 06 B6 43 E8 88 30 2E FC 8D
 3E 95 1E 3E B4 68 4A DB 5C 05 7B 8F 8C 89 B6 CC
 0D EE D1 00 06 5B 51 8A 1C 71 7F 76 82 FF 61 2B
 BC 79 8E C7 B2 49 0F B7 00 3F 94 33 87 37 1C 1D
K_B:
 53 24 DE F8 48 B6 63 CC 26 42 2F 5E 45 EE C3 4C
 51 D2 43 61 B1 65 60 CA 58 A3 D3 28 45 86 CB 7A
beta*P:
  X = 0x238B38644E440452A99FA6B93D9FD7DA0CB83C32D3C1E3CFE5DF5C3EB0F9DB91
    E588DAEDC849EA2FB867AE855A21B4077353C0794716A6480995113D8C20C7AF
  Y = 0xB2273D5734C1897F8D15A7008B862938C8C74CA7E877423D95243EB7EBD02FD2
    C456CF9FC956F078A59AA86F19DD1075E5167E4ED35208718EA93161C530ED14
u_2:
  X = 0xC33844126216E81B372001E77C1FE9C7547F9223CF7BB865C4472EC18BE0C79A
    678CC5AE4028E3F3620CCE355514F1E589F8A0C433CEAF CBD2EE87884D953411
  Y = 0x8B520D083AAF257E8A54EC90CBADBAF4FEED2C2D868C82FF04FCBB9EF6F38E56
    F6BAF9472D477414DA7E36F538ED223D2E2EE02FAE1A20A98C5A9FCF03B6F30D
```

When processing `u_2` and calculating the key on subject A, the `K_A` key takes the following values:

```
K_A:
 53 24 DE F8 48 B6 63 CC 26 42 2F 5E 45 EE C3 4C
 51 D2 43 61 B1 65 60 CA 58 A3 D3 28 45 86 CB 7A
```

The message `MAC_A = HMAC(K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)` from subject A takes the following values:

```
MAC_A:
 E8 EF 9E A8 F1 E6 B1 26 68 E5 8C D2 2D D8 EE C6
 4A 16 71 00 39 FA A6 B6 03 99 22 20 FA FE 56 14
```

The message `MAC_B = HMAC(K_B, 0x02 || ID_B || ind || salt || u_1 || u_2)` from subject B takes the following values:

```
MAC_B:
 61 14 34 60 83 6B 23 5C EC D0 B4 9B 58 7E A4 5D
 51 3C 3A 38 78 3F 1C 9D 3B 05 97 0A 95 6A 55 BA
```

#### A.2.5. Curve id-tc26-gost-3410-2012-512-paramSetB

The input protocol parameters in this example take the following values:

```
N = 1
ind = 1
ID_A:
 00 00 00 00
ID_B:
 00 00 00 00
PW:
 31 32 33 34 35 36 ('123456')
salt:
 29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q_ind:
X = 0x7E1FAE8285E035BEC244BEF2D0E5EBF436633CF50E55231DEA9C9CF21D4C8C33
  DF85D4305DE92971F0A4B4C07E00D87BDBC720EB66E49079285AAF12E0171149
Y = 0x2CC89998B875D4463805BA0D858A196592DB20AB161558FF2F4EF7A85725D209
  53967AE621AFDEAE89BB77C83A2528EF6FCE02F68BDA4679D7F2704947DBC408
```

The function  $F(\text{PW}, \text{salt}, 2000)$  takes the following values:

$F(\text{PW}, \text{salt}, 2000)$ :

```
BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
1C 62 13 E3 93 0E FD DA 26 45 17 92 C6 20 81 22
EE 60 D2 00 52 0D 69 5D FD 9F 5F 0F D5 AB A7 02
```

The coordinates of the point  $Q_{\text{PW}}$  are:

```
X = 0x7D03E65B8050D1E12CBB601A17B9273B0E728F5021CD47C8A4DD822E4627BA5F
    9C696286A2CDDA9A065509866B4DEDEDC4A118409604AD549F87A60AFA621161
Y = 0x16037DAD45421EC50B00D50BDC6AC3B85348BC1D3A2F85DB27C3373580FEF87C
    2C743B7ED30F22BE22958044E716F93A61CA3213A361A2797A16A3AE62957377
```

During the calculation of  $u_1$  on subject A, the parameter alpha, the point  $\text{alpha} \cdot P$ , and  $u_1$  take the following values:

```
alpha=0x715E893FA639BF341296E0623E6D29DADF26B163C278767A7982A989462A3863
    FE12AEF8BD403D59C4DC4720570D4163DB0805C7C10C4E818F9CB785B04B9997
```

$\text{alpha} \cdot P$ :

```
X = 0x10C479EA1C04D3C2C02B0576A9C42D96226FF033C1191436777F66916030D87D
    02FB93738ED7669D07619FFCE7C1F3C4DB5E5DF49E2186D6FA1E2EB5767602B9
Y = 0x039F6044191404E707F26D59D979136A831CCE43E1C5F0600D1DDF8F39D0CA3D
    52FBD943BF04DDCED1AA2CE8F5EBD7487ACDEF239C07D015084D796784F35436
```

$u_1$ :

```
X = 0x45C05CCE8290762F2470B719B4306D62B2911CEB144F7F72EF11D10498C7E921
    FF163FE72044B4E7332AD8CBEC3C12117820F53A60762315BCEB5BC6DA5CF1E0
Y = 0x5BE483E382D0F5F0748C4F6A5045D99E62755B5ACC9554EC4A5B2093E121A2DD
    5C6066BC9EDE39373BA19899208BB419E38B39BBDEDEB0B09A5CAAEEAA984D02E
```

When processing `u_1`, calculating the `K_B` key, and calculating `u_2` on subject B, the parameters `beta`, `src`, `K_B = HASH(src)`, `beta*P`, and `u_2` take the following values:

```
beta=0x30FA8C2B4146C2DBBE82BED04D7378877E8C06753BD0A0FF71EBF2BEFE8DA8F3
      DC0836468E2CE7C5C961281B6505140F8407413F03C2CB1D201EA1286CE30E6D
```

`src`:

```
3F 04 02 E4 0A 9D 59 63 20 5B CD F4 FD 89 77 91
9B BA F4 80 F8 E4 FB D1 25 5A EC E6 ED 57 26 4B
D0 A2 87 98 4F 59 D1 02 04 B5 F4 5E 4D 77 F3 CF
8A 63 B3 1B EB 2D F5 9F 8A F7 3C 20 9C CA 8B 50
B4 18 D8 01 E4 90 AE 13 3F 04 F4 F3 F4 D8 FE 8E
19 64 6A 1B AF 44 D2 36 FC C2 1B 7F 4D 8F C6 A1
E2 9D 6B 69 AC CE ED 4E 62 AB B2 0D AD 78 AC F4
FE B0 ED 83 8E D9 1E 92 12 AB A3 89 71 4E 56 0C
```

`K_B`:

```
D5 90 E0 5E F5 AE CE 8B 7C FB FC 71 BE 45 5F 29
A5 CC 66 6F 85 CD B1 7E 7C C7 16 C5 9F F1 70 E9
```

`beta*P`:

```
X = 0x34C0149E7BB91AE377B02573FCC48AF7BFB7B16DEB8F9CE870F384688E3241A3
  A868588CC0EF4364CCA67D17E3260CD82485C202ADC76F895D5DF673B1788E67
Y = 0x608E944929BD643569ED5189DB871453F13333A1EAF82B2FE1BE8100E775F13D
  D9925BD317B63BFAF05024D4A738852332B64501195C1B2EF789E34F23DDAFC5
```

`u_2`:

```
X = 0x0535F95463444C4594B5A2E14B35760491C670925060B4BEBC97DE3A3076D1A5
  81F89026E04282B040925D9250201024ACA4B2713569B6C3916A6F3344B840AD
Y = 0x40E6C2E55AEC31E7BCB6EA0242857FC6DFB5409803EDF4CA20141F72CC3C7988
  706E076765F4F004340E5294A7F8E53BA59CB67502F0044558C854A7D63FE900
```

When processing `u_2` and calculating the key on subject A, the `K_A` key takes the following values:

`K_A`:

```
D5 90 E0 5E F5 AE CE 8B 7C FB FC 71 BE 45 5F 29
A5 CC 66 6F 85 CD B1 7E 7C C7 16 C5 9F F1 70 E9
```

The message `MAC_A = HMAC(K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)` from subject A takes the following values:

`MAC_A`:

```
DE 46 BB 4C 8C E0 8A 6E F3 B8 DF AC CC 1A 39 B0
8D 8C 27 B6 CB 0F CF 59 23 86 A6 48 F4 E5 BD 8C
```

The message  $MAC\_B = HMAC(K\_B, 0x02 || ID\_B || ind || salt || u\_1 || u\_2)$  from subject B takes the following values:

MAC\_B:

```
EC B1 1D E2 06 1C 55 F1 D1 14 59 CB 51 CE 31 40
99 99 99 2F CA A1 22 2F B1 4F CE AB 96 EE 7A AC
```

#### A.2.6. Curve id-tc26-gost-3410-2012-256-paramSetA

The input protocol parameters in this example take the following values:

N = 1

ind = 1

ID\_A:

```
00 00 00 00
```

ID\_B:

```
00 00 00 00
```

PW:

```
31 32 33 34 35 36 ('123456')
```

salt:

```
29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
```

Q\_ind:

```
X = 0xB51ADF93A40AB15792164FAD3352F95B66369EB2A4EF5EFAE32829320363350E
```

```
Y = 0x74A358CC08593612F5955D249C96AFB7E8B0BB6D8BD2BBE491046650D822BE18
```

The function  $F(PW, salt, 2000)$  takes the following values:

$F(PW, salt, 2000)$ :

```
BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
```

```
D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
```

The coordinates of the point  $Q\_PW$  are:

```
X = 0xDBF99827078956812FA48C6E695DF589DEF1D18A2D4D35A96D75BF6854237629
```

```
Y = 0x9FDDD48BFBC57BEE1DA0CFF282884F284D471B388893C48F5ECB02FC18D67589
```

During the calculation of  $u\_1$  on subject A, the parameter  $\alpha$ , the point  $\alpha * P$ , and  $u\_1$  take the following values:

$\alpha = 0x147B72F6684FB8FD1B418A899F7DBECA5F5FCE60B13685BAA95328654A7F0707F$

$\alpha * P$ :

```
X = 0x33FBAC14EAE538275A769417829C431BD9FA622B6F02427EF55BD60EE6BC2888
```

```
Y = 0x22F2EBCF960A82E6CDB4042D3DDDA511B2FBA925383C2273D952EA2D406EAE46
```

$u\_1$ :

```
X = 0xE569AB544E3A13C41077DE97D659A1B7A13F61DDD808B633A5621FE2583A2C43
```

```
Y = 0xA21A743A08F4D715661297ECD6F86553A808925BF34802BF7EC34C548A40B2C0
```

When processing  $u_1$ , calculating the  $K_B$  key, and calculating  $u_2$  on subject B, the parameters  $\beta$ ,  $\text{src}$ ,  $K_B = \text{HASH}(\text{src})$ ,  $\beta * P$ , and  $u_2$  take the following values:

$\beta = 0x30D5CFADAA0E31B405E6734C03EC4C5DF0F02F4BA25C9A3B320EE6453567B4CB$

$\text{src}$ :

```
A3 39 A0 B8 9C EF 1A 6F FD 4C A1 28 04 9E 06 84
DF 4A 97 75 B6 89 A3 37 84 1B F7 D7 91 20 7F 35
11 86 28 F7 28 8E AA 0F 7E C8 1D A2 0A 24 FF 1E
69 93 C6 3D 9D D2 6A 90 B7 4D D1 A2 66 28 06 63
```

$K_B$ :

```
7D F7 1A C3 27 ED 51 7D 0D E4 03 E8 17 C6 20 4B
C1 91 65 B9 D1 00 2B 9F 10 88 A6 CD A6 EA CF 27
```

$\beta * P$ :

```
X = 0x2B2D89FAB735433970564F2F28CFA1B57D640CB902BC6334A538F44155022CB2
Y = 0x10EF6A82EEF1E70F942AA81D6B4CE5DEC0DDB9447512962874870E6F2849A96F
```

$u_2$ :

```
X = 0x190D2F283F7E861065DB53227D7FBDF429CEBF93791262CB29569BDF63C86CA4
Y = 0xB3F1715721E9221897CCDE046C9B843A8386DBF7818A112F15A02BC820AC8F6D
```

When processing  $u_2$  and calculating the key on subject A, the  $K_A$  key takes the following values:

$K_A$ :

```
7D F7 1A C3 27 ED 51 7D 0D E4 03 E8 17 C6 20 4B
C1 91 65 B9 D1 00 2B 9F 10 88 A6 CD A6 EA CF 27
```

The message  $\text{MAC}_A = \text{HMAC}(K_A, 0x01 || \text{ID}_A || \text{ind} || \text{salt} || u_1 || u_2)$  from subject A takes the following values:

$\text{MAC}_A$ :

```
F9 29 B6 1A 3C 83 39 85 B8 29 F2 68 55 7F A8 11
00 9F 82 0A B1 A7 30 B5 AA 33 4C 3E 6B A3 17 7F
```

The message  $\text{MAC}_B = \text{HMAC}(K_B, 0x02 || \text{ID}_B || \text{ind} || \text{salt} || u_1 || u_2)$  from subject B takes the following values:

$\text{MAC}_B$ :

```
A2 92 8A 5C F6 20 BB C4 90 0D E4 03 F7 FC 59 A5
E9 80 B6 8B E0 46 D0 B5 D9 B4 AE 6A BF A8 0B D6
```

## A.2.7. Curve id-tc26-gost-3410-2012-512-paramSetC

The input protocol parameters in this example take the following values:

```

N = 1
ind = 1
ID_A:
  00 00 00 00
ID_B:
  00 00 00 00
PW:
  31 32 33 34 35 36 ('123456')
salt:
  29 23 BE 84 E1 6C D6 AE 52 90 49 F1 F1 BB E9 EB
Q_ind:
  X = 0x489C91784E02E98F19A803ABCA319917F37689E5A18965251CE2FF4E8D8B298F
    5BA7470F9E0E713487F96F4A8397B3D09A270C9D367EB5E0E6561ADEEB51581D
  Y = 0x684EA885ACA64EAF1B3FEE36C0852A3BE3BD8011B0EF18E203FF87028D6EB5DB
    2C144A0DCC71276542BFD72CA2A43FA4F4939DA66D9A60793C704A8C94E16F18

```

The function  $F(\text{PW}, \text{salt}, 2000)$  takes the following values:

```

F(PW, salt, 2000):
  BD 04 67 3F 71 49 B1 8E 98 15 5B D1 E2 72 4E 71
  D0 09 9A A2 51 74 F7 92 D3 32 6C 6F 18 12 70 67
  1C 62 13 E3 93 0E FD DA 26 45 17 92 C6 20 81 22
  EE 60 D2 00 52 0D 69 5D FD 9F 5F 0F D5 AB A7 02

```

The coordinates of the point  $Q_{\text{PW}}$  are:

```

X = 0x0185AE6271A81BB7F236A955F7CAA26FB63849813C0287D96C83A15AE6B6A864
  67AB13B6D88CE8CD7DC2E5B97FF5F28FAC2C108F2A3CF3DB5515C9E6D7D210E8
Y = 0xED0220F92EF771A71C64ECC77986DB7C03D37B3E2AB3E83F32CE5E074A762EC0
  8253C9E2102B87532661275C4B1D16D2789CDABC58ACFDF7318DE70AB64F09B8

```

During the calculation of  $u_1$  on subject A, the parameter  $\alpha$ , the point  $\alpha * P$ , and  $u_1$  take the following values:

```

alpha=0x332F930421D14CFE260042159F18E49FD5A54167E94108AD80B1DE60B13DE799
  9A34D611E63F3F870E5110247DF8EC7466E648ACF385E52CCB889ABF491EDFF0
alpha*P:
  X = 0x561655966D52952E805574F4281F1ED3A2D498932B00CBA9DECB42837F09835B
    FFBFE2D84D6B6B242FE7B57F92E1A6F2413E12DDD6383E4437E13D72693469AD
  Y = 0xF6B18328B2715BD7F4178615273A36135BC0BF62F7D8BB9F080164AD36470AD0
    3660F51806C64C6691BADEF30F793720F8E3FEAED631D6A54A4C372DCBF80E82

```

u\_1:

```
X = 0x40645B4B9A908D74DEF98886A336F98BAE6ADA4C1AC9B7594A33D5E4A16486C5
533C7F3C5DD84797AB5B4340BFC70CAF1011B69A01A715E5B9B5432D5151CBD7
Y = 0x267FBB18D0B79559D1875909F2A15F7B49ECD8ED166CF7F4FCD1F44891550483
5E80D52BE8D34ADA5B5E159CF52979B1BCFE8F5048DC443A0983AA19192B8407
```

When processing u\_1, calculating the K\_B key, and calculating u\_2 on subject B, the parameters beta, src, K\_B = HASH(src), beta\*P, and u\_2 take the following values:

```
beta=0x38481771E7D054F96212686B613881880BD8A6C89DDEC656178F014D2C093432
A033EE10415F13A160D44C2AD61E6E2E05A7F7EC286BCEA3EA4D4D53F8634FA2
```

src:

```
4F 4D 64 B5 D0 70 08 E9 E6 85 87 4F 88 2C 3E 1E
60 A6 67 5E ED 42 1F C2 34 16 3F DE B4 4C 69 18
B7 BC CE AB 88 A0 F3 FB 78 8D A8 DB 10 18 51 FF
1A 41 68 22 BA 37 C3 53 CE C4 C5 A5 23 95 B7 72
AC 93 C0 54 E3 F4 05 5C ED 6F F0 BE E4 A6 A2 4E
D6 8B 86 FE FA 70 DE 4A 2B 16 08 51 42 A4 DF F0
5D 32 EC 7D DF E3 04 F5 C7 04 FD FA 06 0F 64 E9
E8 32 14 00 25 F3 92 E5 03 50 77 0E 3F B6 2C AC
```

K\_B:

```
A0 83 84 A6 2F 4B E1 AE 48 98 FC A3 6D AA 3F AA
45 1B 3E C5 B5 9C E3 75 F8 9E 92 9F 4B 13 25 8C
```

beta\*P:

```
X = 0xB7C5818687083433BC1AFF61CB5CA79E38232025E0C1F123B8651E62173CE687
3F3E6FFE7281C2E45F4F524F66B0C263616ED08FD210AC4355CA3292B51D71C3
Y = 0x497F14205DBDC89BDDAF50520ED3B1429AD30777310186BE5E68070F016A44E0
C766DB08E8AC23FBDFDE6D675AA4DF591EB18BA0D348DF7AA40973A2F1DCFA55
```

u\_2:

```
X = 0xB772FD97D6FDEC1DA0771BC059B3E5ADF9858311031EAE5AEC6A6EC8104B4105
C45A6C65689A8EE636C687DB62CC0AFC9A48CA66E381286CC73F374C1DD8F445
Y = 0xC64F69425FFEB2995130E85A08EDC3A686EC28EE6E8469F7F09BD3BCBDD843AC
573578DA6BA1CB3F5F069F205233853F06255C4B28586C9A1643537497B1018C
```

When processing u\_2 and calculating the key on subject A, the K\_A key takes the following values:

K\_A:

```
A0 83 84 A6 2F 4B E1 AE 48 98 FC A3 6D AA 3F AA
45 1B 3E C5 B5 9C E3 75 F8 9E 92 9F 4B 13 25 8C
```

The message MAC\_A = HMAC(K\_A, 0x01 || ID\_A || ind || salt || u\_1 || u\_2) from subject A takes the following values:

MAC\_A:

```
12 63 F2 89 0E 90 EE 42 6B 9B A0 8A B9 EA 7F 1F
FF 26 E1 60 5C C6 5D E2 96 96 91 15 E5 31 76 87
```









```

def str2list( s ):
    res = []
    for c in s:
        res += [ ord( c ) ]
    return res

def list2str( l ):
    r = ""
    for k in l:
        r += chr( k )
    return r

def hprint( data ):
    r = ""
    for i in range( len( data ) ):
        r += "%02X " % data[ i ]
        if i % 16 == 15:
            r += "\n"
    print( r )

class Stribog:
    __A = [
        0x8e20faa72ba0b470, 0x47107ddd9b505a38, 0xad08b0e0c3282d1c,
        0xd8045870ef14980e, 0x6c022c38f90a4c07, 0x3601161cf205268d,
        0x1b8e0b0e798c13c8, 0x83478b07b2468764, 0xa011d380818e8f40,
        0x5086e740ce47c920, 0x2843fd2067adea10, 0x14aff010bdd87508,
        0x0ad97808d06cb404, 0x05e23c0468365a02, 0x8c711e02341b2d01,
        0x46b60f011a83988e, 0x90dab52a387ae76f, 0x486dd4151c3dfdb9,
        0x24b86a840e90f0d2, 0x125c354207487869, 0x092e94218d243cba,
        0x8a174a9ec8121e5d, 0x4585254f64090fa0, 0xacc9ca9328a8950,
        0x9d4df05d5f661451, 0xc0a878a0a1330aa6, 0x60543c50de970553,
        0x302a1e286fc58ca7, 0x18150f14b9ec46dd, 0x0c84890ad27623e0,
        0x0642ca05693b9f70, 0x0321658cba93c138, 0x86275df09ce8aaa8,
        0x439da0784e745554, 0xafc0503c273aa42a, 0xd960281e9d1d5215,
        0xe230140fc0802984, 0x71180a8960409a42, 0xb60c05ca30204d21,
        0x5b068c651810a89e, 0x456c34887a3805b9, 0xac361a443d1c8cd2,
        0x561b0d22900e4669, 0x2b838811480723ba, 0x9bcf4486248d9f5d,
        0xc3e9224312c8c1a0, 0xeffa11af0964ee50, 0xf97d86d98a327728,
        0xe4fa2054a80b329c, 0x727d102a548b194e, 0x39b008152acb8227,
        0x9258048415eb419d, 0x492c024284fbaec0, 0xaa16012142f35760,
        0x550b8e9e21f7a530, 0xa48b474f9ef5dc18, 0x70a6a56e2440598e,
        0x3853dc371220a247, 0x1ca76e95091051ad, 0x0edd37c48a08a6d8,
        0x07e095624504536c, 0x8d70c431ac02a736, 0xc83862965601dd1b,
        0x641c314b2b8ee083
    ]

```

```
__Sbox = [  
  0xFC, 0xEE, 0xDD, 0x11, 0xCF, 0x6E, 0x31, 0x16, 0xFB, 0xC4, 0xFA,  
  0xDA, 0x23, 0xC5, 0x04, 0x4D, 0xE9, 0x77, 0xF0, 0xDB, 0x93, 0x2E,  
  0x99, 0xBA, 0x17, 0x36, 0xF1, 0xBB, 0x14, 0xCD, 0x5F, 0xC1, 0xF9,  
  0x18, 0x65, 0x5A, 0xE2, 0x5C, 0xEF, 0x21, 0x81, 0x1C, 0x3C, 0x42,  
  0x8B, 0x01, 0x8E, 0x4F, 0x05, 0x84, 0x02, 0xAE, 0xE3, 0x6A, 0x8F,  
  0xA0, 0x06, 0x0B, 0xED, 0x98, 0x7F, 0xD4, 0xD3, 0x1F, 0xEB, 0x34,  
  0x2C, 0x51, 0xEA, 0xC8, 0x48, 0xAB, 0xF2, 0x2A, 0x68, 0xA2, 0xFD,  
  0x3A, 0xCE, 0xCC, 0xB5, 0x70, 0x0E, 0x56, 0x08, 0x0C, 0x76, 0x12,  
  0xBF, 0x72, 0x13, 0x47, 0x9C, 0xB7, 0x5D, 0x87, 0x15, 0xA1, 0x96,  
  0x29, 0x10, 0x7B, 0x9A, 0xC7, 0xF3, 0x91, 0x78, 0x6F, 0x9D, 0x9E,  
  0xB2, 0xB1, 0x32, 0x75, 0x19, 0x3D, 0xFF, 0x35, 0x8A, 0x7E, 0x6D,  
  0x54, 0xC6, 0x80, 0xC3, 0xBD, 0x0D, 0x57, 0xDF, 0xF5, 0x24, 0xA9,  
  0x3E, 0xA8, 0x43, 0xC9, 0xD7, 0x79, 0xD6, 0xF6, 0x7C, 0x22, 0xB9,  
  0x03, 0xE0, 0x0F, 0xEC, 0xDE, 0x7A, 0x94, 0xB0, 0xBC, 0xDC, 0xE8,  
  0x28, 0x50, 0x4E, 0x33, 0x0A, 0x4A, 0xA7, 0x97, 0x60, 0x73, 0x1E,  
  0x00, 0x62, 0x44, 0x1A, 0xB8, 0x38, 0x82, 0x64, 0x9F, 0x26, 0x41,  
  0xAD, 0x45, 0x46, 0x92, 0x27, 0x5E, 0x55, 0x2F, 0x8C, 0xA3, 0xA5,  
  0x7D, 0x69, 0xD5, 0x95, 0x3B, 0x07, 0x58, 0xB3, 0x40, 0x86, 0xAC,  
  0x1D, 0xF7, 0x30, 0x37, 0x6B, 0xE4, 0x88, 0xD9, 0xE7, 0x89, 0xE1,  
  0x1B, 0x83, 0x49, 0x4C, 0x3F, 0xF8, 0xFE, 0x8D, 0x53, 0xAA, 0x90,  
  0xCA, 0xD8, 0x85, 0x61, 0x20, 0x71, 0x67, 0xA4, 0x2D, 0x2B, 0x09,  
  0x5B, 0xCB, 0x9B, 0x25, 0xD0, 0xBE, 0xE5, 0x6C, 0x52, 0x59, 0xA6,  
  0x74, 0xD2, 0xE6, 0xF4, 0xB4, 0xC0, 0xD1, 0x66, 0xAF, 0xC2, 0x39,  
  0x4B, 0x63, 0xB6  
]
```

```
__Tau = [  
  0,  8, 16, 24, 32, 40, 48, 56,  
  1,  9, 17, 25, 33, 41, 49, 57,  
  2, 10, 18, 26, 34, 42, 50, 58,  
  3, 11, 19, 27, 35, 43, 51, 59,  
  4, 12, 20, 28, 36, 44, 52, 60,  
  5, 13, 21, 29, 37, 45, 53, 61,  
  6, 14, 22, 30, 38, 46, 54, 62,  
  7, 15, 23, 31, 39, 47, 55, 63  
]
```

```

__C = [
  [
    0xb1, 0x08, 0x5b, 0xda, 0x1e, 0xca, 0xda, 0xe9,
    0xeb, 0xcb, 0x2f, 0x81, 0xc0, 0x65, 0x7c, 0x1f,
    0x2f, 0x6a, 0x76, 0x43, 0x2e, 0x45, 0xd0, 0x16,
    0x71, 0x4e, 0xb8, 0x8d, 0x75, 0x85, 0xc4, 0xfc,
    0x4b, 0x7c, 0xe0, 0x91, 0x92, 0x67, 0x69, 0x01,
    0xa2, 0x42, 0x2a, 0x08, 0xa4, 0x60, 0xd3, 0x15,
    0x05, 0x76, 0x74, 0x36, 0xcc, 0x74, 0x4d, 0x23,
    0xdd, 0x80, 0x65, 0x59, 0xf2, 0xa6, 0x45, 0x07
  ],
  [
    0x6f, 0xa3, 0xb5, 0x8a, 0xa9, 0x9d, 0x2f, 0x1a,
    0x4f, 0xe3, 0x9d, 0x46, 0x0f, 0x70, 0xb5, 0xd7,
    0xf3, 0xfe, 0xea, 0x72, 0x0a, 0x23, 0x2b, 0x98,
    0x61, 0xd5, 0x5e, 0x0f, 0x16, 0xb5, 0x01, 0x31,
    0x9a, 0xb5, 0x17, 0x6b, 0x12, 0xd6, 0x99, 0x58,
    0x5c, 0xb5, 0x61, 0xc2, 0xdb, 0x0a, 0xa7, 0xca,
    0x55, 0xdd, 0xa2, 0x1b, 0xd7, 0xcb, 0xcd, 0x56,
    0xe6, 0x79, 0x04, 0x70, 0x21, 0xb1, 0x9b, 0xb7
  ],
  [
    0xf5, 0x74, 0xdc, 0xac, 0x2b, 0xce, 0x2f, 0xc7,
    0x0a, 0x39, 0xfc, 0x28, 0x6a, 0x3d, 0x84, 0x35,
    0x06, 0xf1, 0x5e, 0x5f, 0x52, 0x9c, 0x1f, 0x8b,
    0xf2, 0xea, 0x75, 0x14, 0xb1, 0x29, 0x7b, 0x7b,
    0xd3, 0xe2, 0x0f, 0xe4, 0x90, 0x35, 0x9e, 0xb1,
    0xc1, 0xc9, 0x3a, 0x37, 0x60, 0x62, 0xdb, 0x09,
    0xc2, 0xb6, 0xf4, 0x43, 0x86, 0x7a, 0xdb, 0x31,
    0x99, 0x1e, 0x96, 0xf5, 0x0a, 0xba, 0x0a, 0xb2
  ],
  [
    0xef, 0x1f, 0xdf, 0xb3, 0xe8, 0x15, 0x66, 0xd2,
    0xf9, 0x48, 0xe1, 0xa0, 0x5d, 0x71, 0xe4, 0xdd,
    0x48, 0x8e, 0x85, 0x7e, 0x33, 0x5c, 0x3c, 0x7d,
    0x9d, 0x72, 0x1c, 0xad, 0x68, 0x5e, 0x35, 0x3f,
    0xa9, 0xd7, 0x2c, 0x82, 0xed, 0x03, 0xd6, 0x75,
    0xd8, 0xb7, 0x13, 0x33, 0x93, 0x52, 0x03, 0xbe,
    0x34, 0x53, 0xea, 0xa1, 0x93, 0xe8, 0x37, 0xf1,
    0x22, 0x0c, 0xbe, 0xbc, 0x84, 0xe3, 0xd1, 0x2e
  ],
],

```

```
[
  0x4b, 0xea, 0x6b, 0xac, 0xad, 0x47, 0x47, 0x99,
  0x9a, 0x3f, 0x41, 0x0c, 0x6c, 0xa9, 0x23, 0x63,
  0x7f, 0x15, 0x1c, 0x1f, 0x16, 0x86, 0x10, 0x4a,
  0x35, 0x9e, 0x35, 0xd7, 0x80, 0x0f, 0xff, 0xbd,
  0xbf, 0xcd, 0x17, 0x47, 0x25, 0x3a, 0xf5, 0xa3,
  0xdf, 0xff, 0x00, 0xb7, 0x23, 0x27, 0x1a, 0x16,
  0x7a, 0x56, 0xa2, 0x7e, 0xa9, 0xea, 0x63, 0xf5,
  0x60, 0x17, 0x58, 0xfd, 0x7c, 0x6c, 0xfe, 0x57
],
[
  0xae, 0x4f, 0xae, 0xae, 0x1d, 0x3a, 0xd3, 0xd9,
  0x6f, 0xa4, 0xc3, 0x3b, 0x7a, 0x30, 0x39, 0xc0,
  0x2d, 0x66, 0xc4, 0xf9, 0x51, 0x42, 0xa4, 0x6c,
  0x18, 0x7f, 0x9a, 0xb4, 0x9a, 0xf0, 0x8e, 0xc6,
  0xcf, 0xfa, 0xa6, 0xb7, 0x1c, 0x9a, 0xb7, 0xb4,
  0x0a, 0xf2, 0x1f, 0x66, 0xc2, 0xbe, 0xc6, 0xb6,
  0xbf, 0x71, 0xc5, 0x72, 0x36, 0x90, 0x4f, 0x35,
  0xfa, 0x68, 0x40, 0x7a, 0x46, 0x64, 0x7d, 0x6e
],
[
  0xf4, 0xc7, 0x0e, 0x16, 0xee, 0xaa, 0xc5, 0xec,
  0x51, 0xac, 0x86, 0xfe, 0xbf, 0x24, 0x09, 0x54,
  0x39, 0x9e, 0xc6, 0xc7, 0xe6, 0xbf, 0x87, 0xc9,
  0xd3, 0x47, 0x3e, 0x33, 0x19, 0x7a, 0x93, 0xc9,
  0x09, 0x92, 0xab, 0xc5, 0x2d, 0x82, 0x2c, 0x37,
  0x06, 0x47, 0x69, 0x83, 0x28, 0x4a, 0x05, 0x04,
  0x35, 0x17, 0x45, 0x4c, 0xa2, 0x3c, 0x4a, 0xf3,
  0x88, 0x86, 0x56, 0x4d, 0x3a, 0x14, 0xd4, 0x93
],
[
  0x9b, 0x1f, 0x5b, 0x42, 0x4d, 0x93, 0xc9, 0xa7,
  0x03, 0xe7, 0xaa, 0x02, 0x0c, 0x6e, 0x41, 0x41,
  0x4e, 0xb7, 0xf8, 0x71, 0x9c, 0x36, 0xde, 0x1e,
  0x89, 0xb4, 0x44, 0x3b, 0x4d, 0xdb, 0xc4, 0x9a,
  0xf4, 0x89, 0x2b, 0xcb, 0x92, 0x9b, 0x06, 0x90,
  0x69, 0xd1, 0x8d, 0x2b, 0xd1, 0xa5, 0xc4, 0x2f,
  0x36, 0xac, 0xc2, 0x35, 0x59, 0x51, 0xa8, 0xd9,
  0xa4, 0x7f, 0x0d, 0xd4, 0xbf, 0x02, 0xe7, 0x1e
],
```

```
[
  0x37, 0x8f, 0x5a, 0x54, 0x16, 0x31, 0x22, 0x9b,
  0x94, 0x4c, 0x9a, 0xd8, 0xec, 0x16, 0x5f, 0xde,
  0x3a, 0x7d, 0x3a, 0x1b, 0x25, 0x89, 0x42, 0x24,
  0x3c, 0xd9, 0x55, 0xb7, 0xe0, 0x0d, 0x09, 0x84,
  0x80, 0x0a, 0x44, 0x0b, 0xdb, 0xb2, 0xce, 0xb1,
  0x7b, 0x2b, 0x8a, 0x9a, 0xa6, 0x07, 0x9c, 0x54,
  0x0e, 0x38, 0xdc, 0x92, 0xcb, 0x1f, 0x2a, 0x60,
  0x72, 0x61, 0x44, 0x51, 0x83, 0x23, 0x5a, 0xdb
],
[
  0xab, 0xbe, 0xde, 0xa6, 0x80, 0x05, 0x6f, 0x52,
  0x38, 0x2a, 0xe5, 0x48, 0xb2, 0xe4, 0xf3, 0xf3,
  0x89, 0x41, 0xe7, 0x1c, 0xff, 0x8a, 0x78, 0xdb,
  0x1f, 0xff, 0xe1, 0x8a, 0x1b, 0x33, 0x61, 0x03,
  0x9f, 0xe7, 0x67, 0x02, 0xaf, 0x69, 0x33, 0x4b,
  0x7a, 0x1e, 0x6c, 0x30, 0x3b, 0x76, 0x52, 0xf4,
  0x36, 0x98, 0xfa, 0xd1, 0x15, 0x3b, 0xb6, 0xc3,
  0x74, 0xb4, 0xc7, 0xfb, 0x98, 0x45, 0x9c, 0xed
],
[
  0x7b, 0xcd, 0x9e, 0xd0, 0xef, 0xc8, 0x89, 0xfb,
  0x30, 0x02, 0xc6, 0xcd, 0x63, 0x5a, 0xfe, 0x94,
  0xd8, 0xfa, 0x6b, 0xbb, 0xeb, 0xab, 0x07, 0x61,
  0x20, 0x01, 0x80, 0x21, 0x14, 0x84, 0x66, 0x79,
  0x8a, 0x1d, 0x71, 0xef, 0xea, 0x48, 0xb9, 0xca,
  0xef, 0xba, 0xcd, 0x1d, 0x7d, 0x47, 0x6e, 0x98,
  0xde, 0xa2, 0x59, 0x4a, 0xc0, 0x6f, 0xd8, 0x5d,
  0x6b, 0xca, 0xa4, 0xcd, 0x81, 0xf3, 0x2d, 0x1b
],
[
  0x37, 0x8e, 0xe7, 0x67, 0xf1, 0x16, 0x31, 0xba,
  0xd2, 0x13, 0x80, 0xb0, 0x04, 0x49, 0xb1, 0x7a,
  0xcd, 0xa4, 0x3c, 0x32, 0xbc, 0xdf, 0x1d, 0x77,
  0xf8, 0x20, 0x12, 0xd4, 0x30, 0x21, 0x9f, 0x9b,
  0x5d, 0x80, 0xef, 0x9d, 0x18, 0x91, 0xcc, 0x86,
  0xe7, 0x1d, 0xa4, 0xaa, 0x88, 0xe1, 0x28, 0x52,
  0xfa, 0xf4, 0x17, 0xd5, 0xd9, 0xb2, 0x1b, 0x99,
  0x48, 0xbc, 0x92, 0x4a, 0xf1, 0x1b, 0xd7, 0x20
]
]
```



```

def __AddModulo(self, A, B):
    result = [0] * 64
    t = 0
    for i in reversed(range(0, 64)):
        t = A[i] + B[i] + (t >> 8)
        result[i] = t & 0xFF
    return result

def __AddXor(self, A, B):
    result = [0] * 64
    for i in range(0, 64):
        result[i] = A[i] ^ B[i]
    return result

def __S(self, state):
    result = [0] * 64
    for i in range(0, 64):
        result[i] = self.__Sbox[state[i]]
    return result

def __P(self, state):
    result = [0] * 64
    for i in range(0, 64):
        result[i] = state[self.__Tau[i]]
    return result

def __L(self, state):
    result = [0] * 64
    for i in range(0, 8):
        t = 0
        for k in range(0, 8):
            for j in range(0, 8):
                if ((state[i * 8 + k] & (1 << (7 - j))) != 0):
                    t ^= self.__A[k * 8 + j]
            for k in range(0, 8):
                result[i * 8 + k] = (t & (0xFF << (7 - k) * 8)) >> (7 - k) * 8
    return result

def __KeySchedule(self, K, i):
    K = self.__AddXor(K, self.__C[i])
    K = self.__S(K)
    K = self.__P(K)
    K = self.__L(K)
    return K

```

```

# E(K, m)
def __E(self, K, m):
    state = self.__AddXor(K, m)
    for i in range(0, 12):
        state = self.__S(state)
        state = self.__P(state)
        state = self.__L(state)
        K = self.__KeySchedule(K, i)
        state = self.__AddXor(state, K)
    return state

def __G_n(self, N, h, m):
    K = self.__AddXor(h, N)
    K = self.__S(K)
    K = self.__P(K)
    K = self.__L(K)
    t = self.__E(K, m)
    t = self.__AddXor(t, h)
    return self.__AddXor(t, m)

def __Padding(self, last, N, h, Sigma):
    if (len(last) < 64):
        padding = [0] * (64 - len(last))
        padding[-1] = 1
        padded_message = padding + last
    h = self.__G_n(N, h, padded_message)
    N_len = [0] * 64
    N_len[63] = (len(last) * 8) & 0xff
    N_len[62] = (len(last) * 8) >> 8
    N = self.__AddModulo(N, N_len)
    Sigma = self.__AddModulo(Sigma, padded_message)
    return (h, N, Sigma)

def digest( self, message, out=512 ):
    return list2str( self.GetHash( str2list( message ), out ) )

def GetHash(self, message, out=512, no_pad=False):
    N = [0] * 64
    Sigma = [0] * 64
    if out == 512:
        h = [0] * 64
    elif out == 256:
        h = [0x01] * 64
    else:
        print("Wrong hash out length!")

    N_512 = [0] * 64
    N_512[62] = 0x02    # 512 = 0x200

```

```

length_bits = len(message) * 8
length = len(message)

i = 0
asd = message[::-1]
while (length_bits >= 512):
    tmp = (message[i * 64: (i + 1) * 64])[::-1]
    h = self.__G_n(N, h, tmp)
    N = self.__AddModulo(N, N_512)
    Sigma = self.__AddModulo(Sigma, tmp)
    length_bits -= 512
    i += 1

last = (message[i * 64: length])[::-1]

if (len(last) == 0 and no_pad):
    pass
else:
    h, N, Sigma = self.__Padding(last, N, h, Sigma)

N_0 = [0] * 64
h = self.__G_n(N_0, h, N)
h = self.__G_n(N_0, h, Sigma)

if out == 512:
    return h[::-1]
elif out == 256:
    return (h[0:32])[::-1]

def hash(self, str_message, out=512, no_pad=False):
    return list2str(self.GetHash(str2list(str_message), out, no_pad))

def H256(msg):
    S = Stribog()
    return S.hash(msg, out=256)

def H512(msg):
    S = Stribog()
    return S.hash(msg)

def num2le( s, n ):
    res = ""
    for i in range(n):
        res += chr(s & 0xFF)
        s >>= 8
    return res

```

```

def le2num( s ):
    res = 0
    for i in range(len(s) - 1, -1, -1):
        res = (res << 8) + ord(s[i])
    return res

def XGCD(a,b):
    """XGCD(a,b) returns a list of form [g,x,y], where g is GCD(a,b) and
    x,y satisfy the equation g = ax + by."""
    a1=1; b1=0; a2=0; b2=1; aneg=1; bneg=1; swap = False
    if(a < 0):
        a = -a; aneg=-1
    if(b < 0):
        b = -b; bneg=-1
    if(b > a):
        swap = True
        [a,b] = [b,a]
    while (1):
        quot = -(a / b)
        a = a % b
        a1 = a1 + quot*a2; b1 = b1 + quot*b2
        if(a == 0):
            if(swap):
                return [b, b2*bneg, a2*aneg]
            else:
                return [b, a2*aneg, b2*bneg]
        quot = -(b / a)
        b = b % a
        a2 = a2 + quot*a1; b2 = b2 + quot*b1
        if(b == 0):
            if(swap):
                return [a, b1*bneg, a1*aneg]
            else:
                return [a, a1*aneg, b1*bneg]

def getMultByMask( elems, mask ):
    n = len( elems )
    r = 1
    for i in range( n ):
        if mask & 1:
            r *= elems[ n - 1 - i ]
        mask = mask >> 1
    return r

```

```
def subF(P, other, p):
    return (P - other) % p

def divF(P, other, p):
    return mulF(P, invF(other, p), p)

def addF(P, other, p):
    return (P + other) % p

def mulF(P, other, p):
    return (P * other) % p

def invF(R, p):
    assert (R != 0)
    return XGCD(R, p)[1] % p

def negF(R, p):
    return (-R) % p

def powF(R, m, p):
    assert R != None
    assert type(m) in (int, long)

    if m == 0:
        assert R != 0
        return 1
    elif m < 0:
        t = invF(R, p)
        return powF(t, (-m), p)
    else:
        i = m.bit_length() - 1
        r = 1
        while i > 0:
            if (m >> i) & 1:
                r = (r * R) % p
            r = (r * r) % p
            i -= 1
        if m & 1:
            r = (r * R) % p
        return r
```

```
def add(Px, Py, Qx, Qy, p, a, b):
    if Qx == Qy == None:
        return [Px, Py]

    if Px == Py == None:
        return [Qx, Qy]

    if (Px == Qx) and (Py == negF(Qy, p)):
        return [None, None]

    if (Px == Qx) and (Py == Qy):
        assert Py != 0
        return duplicate(Px, Py, p, a)
    else:
        l = divF( subF( Qy, Py, p ), subF( Qx, Px, p ), p )
        resX = subF( subF( powF( l, 2, p ), Px, p ), Qx, p )
        resY = subF( mulF( l, subF( Px, resX, p ), p ), Py, p )
        return [resX, resY]

def duplicate(Px, Py, p, a):
    if (Px == None) and (Py == None):
        return [None, None]

    if Py == 0:
        return [None, None]

    l = divF(addF(mulF(powF(Px, 2, p), 3, p), a, p), mulF(Py, 2, p), p)
    resX = subF(powF(l, 2, p), mulF(Px, 2, p), p)
    resY = subF(mulF(l, subF(Px, resX, p), p), Py, p)
    return [resX, resY]
```

```

def mul(Px, Py, s, p, a, b):
    assert type(s) in (int, long)
    assert Px != None and Py != None

    X = Px
    Y = Py

    i = s.bit_length() - 1
    resX = None
    resY = None
    while i > 0:
        if (s >> i) & 1:
            resX, resY = add(resX, resY, X, Y, p, a, b)
            resX, resY = duplicate(resX, resY, p, a)
            i -= 1
        if s & 1:
            resX, resY = add(resX, resY, X, Y, p, a, b)
    return [resX, resY]

def Ord(Px, Py, m, q, p, a, b):
    assert Px != None and Py != None
    assert (m != None) and (q != None)
    assert mul(Px, Py, m, p, a, b) == [None, None]

    X = Px
    Y = Py
    r = m
    for mask in range(1 << len(q)):
        t = getMultByMask(q, mask)
        Rx, Ry = mul(X, Y, t, p, a, b)
        if (Rx == None) and (Ry == None):
            r = min(r, t)
    return r

def isQuadraticResidue( R, p ):
    if R == 0:
        assert False
    temp = powF(R, ((p - 1) / 2), p)
    if temp == (p - 1):
        return False
    else:
        assert temp == 1
        return True

```

```

def getRandomQuadraticNonresidue(p):
    from random import randint
    r = (randint(2, p - 1)) % p
    while isQuadraticResidue(r, p):
        r = (randint(2, p - 1)) % p
    return r

def ModSqrt( R, p ):
    assert R != None
    assert isQuadraticResidue(R, p)

    if p % 4 == 3:
        res = powF(R, (p + 1) / 4, p)
        if powF(res, 2, p) != R:
            res = None
        return [res, negF(res, p)]
    else:
        ainvF = invF(R, p)

        s = p - 1
        alpha = 0
        while (s % 2) == 0:
            alpha += 1
            s = s / 2

        b = powF(getRandomQuadraticNonresidue(p), s, p)
        r = powF(R, (s + 1) / 2, p)

        bj = 1
        for k in range(0, alpha - 1): # alpha >= 2 because p % 4 = 1
            d = 2 ** (alpha - k - 2)
            x = powF(mulF(powF(mulF(bj, r, p), 2, p), ainvF, p), d, p)
            if x != 1:
                bj = mulF(bj, powF(b, (2 ** k), p), p)
        res = mulF(bj, r, p)
        return [res, negF(res, p)]

```



```

def generateQs( p, pByteSize, a, b, m, q, orderDivisors, Px, Py, N ):
    assert pByteSize in ( 256 / 8, 512 / 8 )
    PxBytes = num2le( Px, pByteSize )
    PyBytes = num2le( Py, pByteSize )
    Qs = []
    S = []
    Hash_src = []
    Hash_res = []
    co_factor = m / q

    seed = 0
    while len( Qs ) != N:
        hashSrc = PxBytes + PyBytes + num2le( seed, 4 )
        if pByteSize == ( 256 / 8 ):
            QxBytes = H256( hashSrc )
        else:
            QxBytes = H512( hashSrc )

        Qx = le2num( QxBytes ) % p

        R = addF( addF( powF( Qx, 3, p ), mulF( Qx, a, p ), p ), b, p )
        if ( R == 0 ) or ( not isQuadraticResidue( R, p ) ):
            seed += 1
            continue

        Qy_sqrt = ModSqrt( R, p )
        Qy = min( Qy_sqrt )
        if co_factor * Ord( Qx, Qy, m, orderDivisors, p, a, b ) != m:
            seed += 1
            continue

        Qs += [( Qx, Qy )]
        S += [seed]
        Hash_src += [hashSrc]
        Hash_res += [QxBytes]
        seed += 1

    return Qs, S, Hash_src, Hash_res

```

```

if __name__ == "__main__":
    for i, curve in enumerate(enumerateParams):
        print "A.1." + str(i+1) + ". Curve " + curve["OID"]
        if "3410-2012-256-paramSetA" in curve["OID"] or \
            "3410-2012-512-paramSetC" in curve["OID"]:
            Q, S, Hash_src, Hash_res = generateQs(curve["p"],\
                curve["n"],\
                curve["a"],\
                curve["b"],\
                curve["m"],\
                curve["q"],\
                [ 2, 2, curve["q"]],\
                curve["x"],\
                curve["y"],\
                1)
        else:
            Q, S, Hash_src, Hash_res = generateQs(curve["p"],\
                curve["n"],\
                curve["a"],\
                curve["b"],\
                curve["m"],\
                curve["q"],\
                [curve["q"]],\
                curve["x"],\
                curve["y"],\
                1)

    j = 1
    for q, s, hash_src, hash_res in zip(Q, S, Hash_src, Hash_res):
        print "Point Q_" + str(j)
        j += 1

        print "X=", hex(q[0])[:-1]
        print "Y=", hex(q[1])[:-1]

        print "SEED=", "{0:#0{1}x}".format(s,6)
        print

```

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